

Programming Paradigms

Summer Term 2018

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Organisation

About us

- Lecturer: Prof. Janis Voigtländer, Room LF 233 Area: Formal Methods, Programming Languages
- Teaching Assistant: Marcel Fourné, Room LF 231B
- Student Assistants: Daniel Laybourn Matthias Schaffeld

To my knowledge, mainly:

- 1. Bachelor Students "Angewandte Informatik"
- 2. Bachelor Students "Computer Engineering (ISE)"

Some (relevant) lectures you have presumably attended:

- Grundlegende Programmiertechniken
- Fortgeschrittene Programmiertechniken (?)
- Logik
- Softwaretechnik (?)

This lecture

- Weekly slot: Wednesday, 12:15 – 13:45, in LB 134 about 13 times this term
- Slides will be made available after each lecture.

• There will be other material as well.

• We use the standard UDE Moodle system.

Groups:

- Mon, 16:15 17:45, LE 105 (English, Marcel)
- Tue, 10:15 11:45, LE 120 (German, Daniel)
- Thu, 10:15 11:45, LC 137 (German, Daniel)
- Fri, 08:30 10:00, LE 120 (German, Daniel)

Starting in the third lecture week.

- You can earn bonus points for the exam.
- But mainly, doing the exercises is important to be successful in the course.

- In particular, there will be a focus on programming concepts and tasks. Such material cannot be learned by heart. It needs practice!
- Not all tasks each week will be mandatory/contributing to earning the exam bonus. But you are advised to work on all tasks, and to go to the exercise sessions.

Moodle for:

- Lecture slides and material
- Exercise sheets
- Announcements
- Discussion forum
- Submission of (some) exercises

Course key: ...

- There will be a written exam, tentatively planned for Tue, 28th August.
- Registration for the exam will be via the exam office.
- The exam will be offered in English and German.

• The exam will be about the course as taught this term!

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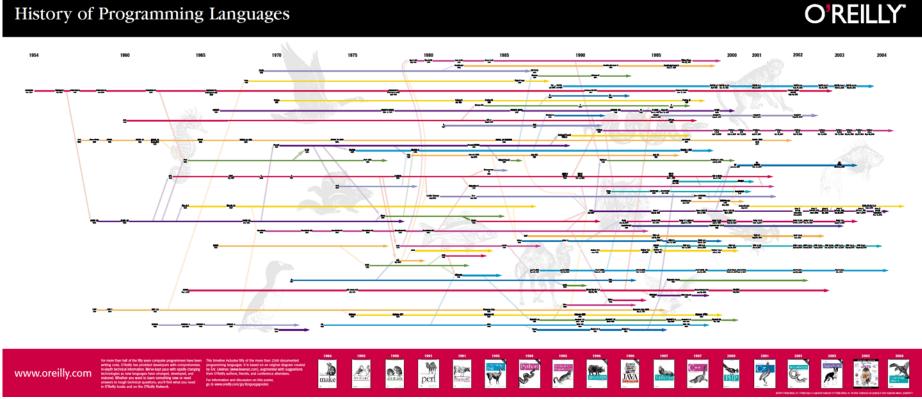
- The course will have a stronger emphasis on programming than in the past, even more so than last year.
- Some content of last year, and of the years before that, will not be covered (formal syntax description, axiomatic semantics of imperative programs, objectorientation).
- The intention is to do more programming also in the lecture.
- But of course, there will still be a lot of continuity.
- As an aside, I have started to produce new slides...

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Introduction / Motivation

"To know another language is to have a second soul." Charlemagne, 747/748 – 814

History of Programming Languages



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12

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Another perspective

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1955 Fortran COBOL Algol 60 Lisp 1960 Snobol BASIC PL/I APL 1965 Simula 67 Logo Forth в Pascal 1970 Prolog ML Scheme С 1975 lcon Smalltalk Ada Modula awk 1980 Miranda Postscript C++ Common Lisp 1985 Haskell Eiffel Perl CLOS J 1990 Python Visual Basic Dylan Lua Ruby Java PHP 1995 kev imperative object-oriented C# functional declarative 2000

From "American Scientist": The Semicolon Wars, © 2006 Brian Hayes

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And yet another one

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Logo Smalltalk Self Lisp JavaScript Dylan AWK Python Lua Perl Common Lisp Forth Ruby Simula Scheme Objective-C CLU Java C++ Oberon Eiffel Ada Modula-3 Modula-2 Erlang Object Pascal APL Prolog ALGOL 68 Scala Pascal C# ALGOL ML ALGOL 60 SQL Haskell C Visual Basic ISWIM BASIC Fortran Speedcoding PL/I COBOL

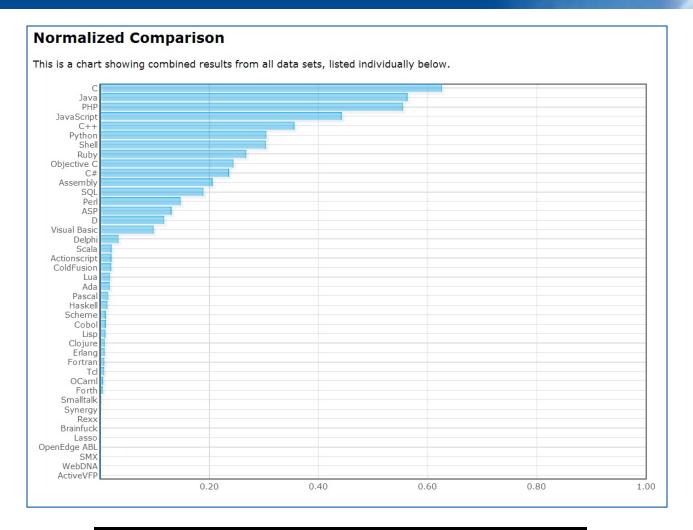
http://preview.tinyurl.com/language-influences

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Also, popularity contests, ...

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http://preview.tinyurl.com/popular-languages

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- Can one language do "more" than others?
- Are there problems that one cannot solve in certain languages?
- Is there a "best" language? At least for a certain purpose or application area?

• What does actually separate different programming languages from each other?

Some relevant distinctions:

- syntactically rich vs. syntactically scarce (e.g., APL vs. Lisp)
- verbosity vs. succinctness (e.g., COBOL vs. Haskell)
- compiled vs. interpreted (e.g., C vs. Perl)
- domain-specific vs. general purpose (e.g., SQL vs. Java)
- sequential vs. concurrent/parallel (e.g., JavaScript vs. Erlang)
- typed vs. untyped (e.g., Haskell vs. Prolog)
- dynamic vs. static (e.g., Ruby vs. ML)
- declarative vs. imperative (e.g., Prolog vs. C)
- object-oriented vs. ???

Approaches to the specification of languages

- ... describing syntax,
- ... describing semantics,

as well as implementation strategies.

Language concepts:

- variables and bindings
- type constructs
- control structures and abstraction features

And, of course, paradigms that span a whole class of languages.

- We will focus on two paradigms: functional and logic programming.
- For each, we pick a specific language: Haskell, Prolog.
- We consider actual programming concepts, and also aspects related to semantics (evaluation, resolution).
- With Haskell, we explore typing concepts like inference, genericity, polymorphism.
- We discuss and compare concepts like variables, statements vs. expressions, etc., in different languages.

- Functional and logic programming are often called "declarative" or "descriptive" programming.
- The idea is that programmers can think more in terms of "What?" instead of "How?", in other words, more in terms of specification than planning a certain computation process.
- Of course, there is still a need for algorithmic thinking etc., as there is no magic.
- But it is true that declarative programming has a more high-level, sometimes mathematical, feel to it.
- Also, the "What-instead-of-How" aspect will become concrete with observations like the roles of expressions vs. statements in different languages/paradigms.
- A side benefit in declarative languages is often reduced syntax.

Other reasons for studying "new" paradigms

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- Learning different languages now makes it easier to pick up new languages later on.
- Concepts from once "exotic" languages make their way into "mainstream" ones.
- In some application domains, there is an increased demand for very disciplined, conceptually expressive, mathematics-based languages.
- Generally, knowing more paradigms increases capacity to express ideas.

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Literature

- Programming in Haskell, 2nd edition; Graham Hutton
- Haskell The Craft of Functional Programming, 3rd edition; Simon Thompson
- Thinking Functionally with Haskell; Richard Bird
- Haskell-Intensivkurs; Marco Block, Adrian Neumann
- Einführung in die Programmierung mit Haskell; Manuel Chakravarty, Gabriele Keller

- Learn Prolog Now!; Patrick Blackburn, Johan Bos, Kristina Striegnitz
- Programmieren in Prolog; William Clocksin, Christopher Mellish
- Prolog Verstehen und Anwenden; Armin Ertl

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A first glimpse of FP with CodeWorld

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import CodeWorld

```
main = animationOf scene
```

```
scene t = pictures $
```

```
[ circle 8
```

```
, colored green (solidRectangle 4 4)
```

```
, rotated (pi/2)
```

```
(translated 8 0 (colored red (polygon [(0,0),(1,0.5),(1,0.5)])))
```

```
1
```

```
++
```

```
[ rotated ((a+t)*pi/20)
```

```
(rectangle (4+a) (4+a)) | a <- [ 0, 0.5 .. 9 ] ]
```

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Expressions vs. statements

Expression-based programming

 Proposition: Functional programming is about expressions, whereas imperative programming is about statements.

• Some kinds of expressions you (probably) know:

 $2+3\cdot(x+1)^2$

 $p \land \neg (q \lor r)$

SUMIF(A1:A8,"<0")

• Generally: terms in any algebra, built from constants and functions/operators, possibly containing variables

Expressions

- ... are compositional, built completely from subexpressions,
- ... often have a meaningful type,
- … have a value, which does not depend on "hidden influences", and does not change on re-evaluation or based on the order of evaluating subexpressions.

The compositionality is not just syntactical (expressions are built from subexpressions), but extends to <u>typing</u> and <u>semantics/evaluation</u>.

Properties of (pure) expressions

Example
$$2 + 3 \cdot (x + 1)^2$$
:

The constants are 1, 2, 3 of type \mathbb{Z} .

The operators are $+: \mathbb{Z} \times \mathbb{Z} \to \mathbb{Z}, \cdot: \mathbb{Z} \times \mathbb{Z} \to \mathbb{Z}, ()^2: \mathbb{Z} \to \mathbb{Z}.$

The value of $2 + 3 \cdot (x + 1)^2$ depends only on the value of 2 and the value of $3 \cdot (x + 1)^2$, the latter only depends on the value of 3 and the value of $(x + 1)^2$, ...

- Thanks to these properties, we can easily use notation known from mathematics, for example reformulating "2 + 3 · (x + 1)²" as follows:
 "2 + 3 · y² where y = x + 1".
- Also, we can apply simplifications, for example replacing exponentiation by multiplication: " $2 + 3 \cdot y \cdot y$ where y = x + 1".
- And while this example was about arithmetic expressions, the concepts apply much more generally.
- But only if we have <u>pure</u> expressions!

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- So what is different in imperative programming?
- Don't we also have expressions there? For example in:

b = 100000; if (z > 0) { z = 100 + z; j = 0; while (b < 200000) { b = b * z / 100; j = j + 1; } } else j = -1;

• Yes, there are expressions, but they are not the dominating syntactical construct. Statements are!

- Why is this difference relevant? What properties do statements, as opposed to expressions, not have?
- Well, for example, they are not even syntactically compositional: Not every well-formed smaller part of a statement is itself a statement.

while (b < 200000) {
 b = b * z / 100;
 j = j + 1;
}</pre>

- Instead, expressions occur, also keywords, ...
- Moreover, statements do not always have a meaningful type.
- Or even just a value. (Try giving a value for the above block.)

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- As a consequence, we cannot name arbitrary well-formed smaller parts (as opposed to what we saw for expressions and their subexpressions).
- For example, we cannot simply write:

```
body = {
    b = b * z / 100;
    j = j + 1;
}
while (b < 200000) body;</pre>
```

• Even workarounds involving functions/procedures/methods are not as flexible and useful as the kind of mathematical notation for expressions: " $2 + 3 \cdot y^2$ where y = x + 1".

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- Okay, so what about the sublanguage of expressions in an imperative language? Can <u>they</u>, at least, be treated as we saw before?
- Not in general! For example, we saw that mathematically we should be able to rewrite something like " $exp_1 + exp_2 \cdot (exp_3)^2$ " as any of:

 $exp_1 + exp_2 \cdot var^2$ where $var = exp_3$ $exp_1 + exp_2 \cdot var \cdot var$ where $var = exp_3$ $exp_1 + exp_2 \cdot exp_3 \cdot exp_3$ where $var = exp_3$

 But code snippets like "result = exp₁ + exp₂ * (exp₃)²;" do not take well to being replaced by:

var = \exp_3 ; result = \exp_1 + \exp_2 * var²;

• ... or by code snippets corresponding to the other expression alternatives above.

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• Indeed, consider these four code snippets:

result = \exp_1 + \exp_2 * $(\exp_3)^2$; var = \exp_3 ; result = \exp_1 + \exp_2 * var^2 ; var = \exp_3 ; result = \exp_1 + \exp_2 * var * var; result = \exp_1 + \exp_2 * \exp_3 * \exp_3 ;

- And imagine instantiations with exp₃ being the "expression" i++ or some invocation f() for a procedure/method f.
- The problem is that expressions in an imperative language are typically not <u>pure</u> expressions. Instead, they have side-effects!
- (For same reason, re-evaluation of an expression can change the value. And order of evaluating subexpressions becomes relevant.)

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- So, how "bad" is all that?
- Do these artificial examples "prove" anything?
- Well, I haven't (yet?) argued that the pure expressionbased style is better in some sense.

 But what should have become clear is that it is <u>different</u>!

• In any case, let us "do" something with CodeWorld.

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Another look at FP with CodeWorld

A rather simple example:

```
main :: IO ()
main = drawingOf scene
```

```
scene :: Picture
```

scene = circle 0.1 & translated 3 0 (colored red triangle)

```
triangle :: Picture
triangle = polygon [(0,0),(1,-0.5),(1,0.5)]
```

Let us discuss this from the "expression" perspective ...

Observations:

- Compositionality on level of syntax, types, and values.
- Pictures are expressions/values here, can be named etc.
- Functions/operators used:

circle	:	$\mathbb{R} \rightarrow \mathtt{Picture}$
polygon	:	$[\mathbb{R} \times \mathbb{R}] \rightarrow \mathtt{Picture}$
colored	:	Color \times Picture \rightarrow Picture
translated	:	\mathbb{R} × \mathbb{R} × Picture \rightarrow Picture
&	:	Picture \times Picture \rightarrow Picture

Properties like: translated a b (colored c d)
 ≡ colored c (translated a b d)

A slight variation:

```
main :: IO ()
main = animationOf scene
scene :: Double -> Picture
scene t = translated t 0 (colored red triangle)
```

- Dependence on time expressed via parameter t.
- That parameter is never set by us for the animation.
- No for-loop or other explicit control.
- Instead, the animationOf construct takes care "somehow" (this involves evaluating scene for different t).

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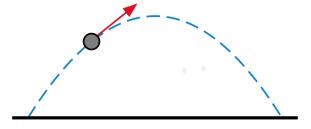
Another example

- Mathematically describing dynamic behaviour as a function of time should not be much of a surprise.
- A well-known physics example:

$$x(t) = v_{0x} \cdot t$$

$$y(t) = v_{0y} \cdot t - \frac{g}{2} \cdot t^2$$

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Rich expressions

A desire for additional expressivity

- In the examples, we have already expressed continuous distribution, throughout time, via functions.
- What if we also, or alternatively, want a discrete distribution, throughout "space"?
- So, instead of one triangle moving in time, we want several static triangles at different places.
- But we do not really want to replicate these "by hand".
- Maybe now is the time for a for-loop?
- No, we don't have that.
- But what do we have instead?

Using a list comprehension:

```
main :: IO ()
main = drawingOf (pictures [ scene d | d <- [0..5] ])
scene :: Double -> Picture
scene d = translated d 0 (colored red triangle)
```

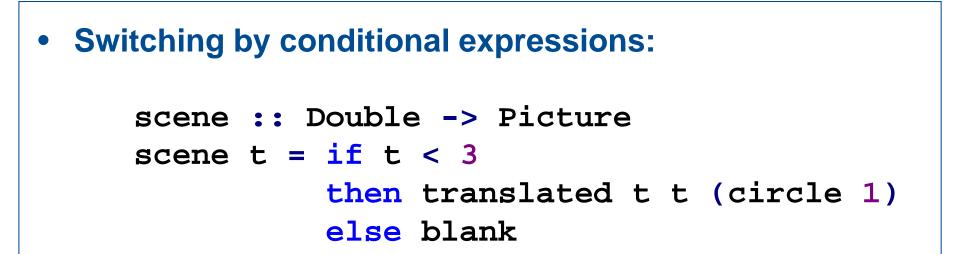
- With pictures :: [Picture] -> Picture.
- And a list comprehension [scene d | d <- [0..5]].
- This is <u>not</u> like a for-loop, for several reasons.
- Instead, it is like a mathematical set comprehension $\{ 2 \cdot n \mid n \in \mathbb{N} \}$.

- Expressions: syntactic structures one could imagine after the "=" in an assignment "var = ..." in C or Java.
- Values: results of evaluating expressions, obtained by combining values of subexpressions.
- Statements: syntactic structures that are characterized not so much by what (if anything at all) they evaluate to, but rather by what effect they have (change of storage cells, looping, etc.).
- In a pure, non-statement setting, any two expressions that have the same value can be replaced for each other, without changing the behaviour of the program.

Some takeaways from examples you have seen:

- Non-constant behaviour expressed as functions, in the mathematical sense. $f(x) = \cdots$
- Such a description defines the behaviour "as a whole", not in a "piecemeal" fashion.
- For example, there is no "first run this piece of animation, then that piece, and then something else".
- Actually, there is not even a concept of "this piece of animation stops at some point".

Of course, we should be able to also express possibly noncontinuous behaviours. But we are <u>not</u> resorting to sequential statements, with imperative keywords or semicolons etc. Instead, ...



• This is very much in line with case distinctions in mathematical functions:

$$f(x) = \begin{cases} -x, & \text{if } x < 0\\ x, & \text{else} \end{cases}$$

We had:

```
main :: IO ()
main = drawingOf (pictures [ scene d | d <- [0..5] ])
scene :: Double -> Picture
scene d = translated d 0 (colored red triangle)
```

- Also <u>this</u> is a "wholemeal" approach, since we express the application of scene to the elements of [0..5] "in one go".
- Specifically, we do not conceptually consider "one after another": the resulting values are completely independent, no individual instance influences any other.
- Just like in the mathematical notation $\{ f(n) \mid n \in \mathbb{N} \}$.

We had:

```
main :: IO ()
main = drawingOf (pictures [ scene d | d <- [0..5] ])
scene :: Double -> Picture
scene d = translated d 0 (colored red triangle)
```

- Of course, the individual evaluations will, on a sequential machine, happen in some order. And the resulting list is really a sequence, not a set. But the individual values will be independent of all that.
- Indeed, one can show that for any f and n, in Haskell:
 [fi|i<-[0..n]]
 ≡ reverse [fi|i<-reverse [0..n]]

 In contrast, it is not remotely true that in an imperative language we can always replace a piece of code written like this:

by this:

 And even for the cases where statements as above <u>are</u> equivalent, a formulation given that way is less useful than the Haskell equation we saw, or indeed its more general version:

Another example, both for list comprehensions and for the pragmatic value of expression-based programming:

• Imagine we have a way to depict a star, e.g.:

star :: Picture
star = polygon [...]

• ... but want to depict a galaxy.

• Let us work on this in CodeWorld, but also try to think about how to do something analogous in Java or so.

```
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More mundane examples of list comprehensions
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> [1,3..10]
[1,3,5,7,9]
> [ x^2 | x < [1..10], even x ]
[4, 16, 36, 64, 100]
> [ y | x <- [1..10], let y = x^2, y `mod` 4 == 0 ]
[4, 16, 36, 64, 100]
> [ x * y | x <- [1,2,3], y <- [1,2,3] ]</pre>
[1,2,3,2,4,6,3,6,9]
```

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>
$$[(x,y) | x < [1,2,3], y < [4,5]]$$

 $[(1,4),(1,5),(2,4),(2,5),(3,4),(3,5)]$

```
> [ (x,y) | y <- [4,5], x <- [1,2,3] ]
[(1,4),(2,4),(3,4),(1,5),(2,5),(3,5)]</pre>
```

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Remarks on syntax and types

Instead of:

circle	:	$\mathbb{R} \rightarrow \mathtt{Picture}$
polygon	:	$[\mathbb{R} \times \mathbb{R}] \rightarrow \texttt{Picture}$
colored	:	Color \times Picture \rightarrow Picture
translated	:	$\mathbb{R} \times \mathbb{R} \times Picture \rightarrow Picture$
&	:	Picture \times Picture \rightarrow Picture

type signatures actually look like this:

circle	::	Double -> Picture
polygon	::	[(Double, Double)] -> Picture
colored	::	Color -> Picture -> Picture
translated	::	Double -> Double -> Picture -> Picture
(&)	::	Picture -> Picture -> Picture

- Instead of f(x) and g(x,y,z), we write f x and g x y z.
- As an example for nested function application, instead of g(x,f(y),z), we write g x (f y) z.
- The same syntax is used at function definition sites, so something like

```
float f(int a, char b)
{ ... }
```

in C or Java would correspond to

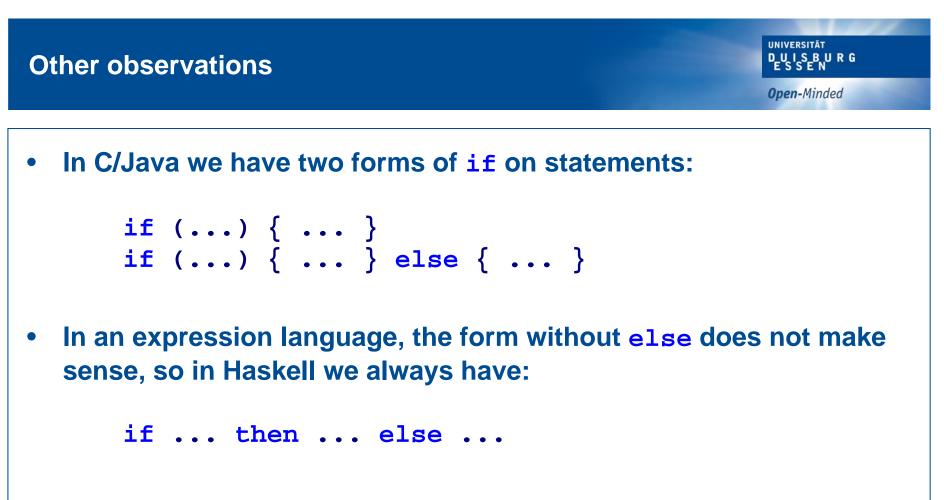
f :: Int -> Char -> Float
f a b = ...

in Haskell.

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• This corresponds to C/Java's conditional operator:

```
....? .... : ....
```

• Pragmatically, an if-then-else expression "without an else" would be realized by having some "neutral value" in the elsebranch. Remember:

```
scene :: Double -> Picture
scene t = if t < 3
    then translated t t (circle 1)
    else blank</pre>
```

- Similarly, in a list context: if condition then list else []
- Also, do not hesitate to use if-then-else as subexpressions freely:

```
f x y (if exp_1 then exp_2 else exp_3)

\equiv if exp_1 then f x y exp_2 else f x y exp_3
```

In Haskell, this:

let y = a * b
 f x = (x + y) / y
in f c + f d

is equivalent to:

let { y = a * b; f x = (x + y) / y }
in f c + f d

But these are not accepted:

let y = a * b
 f x = (x + y) / y
in f c + f d

- Haskell beginners tend to use unnecessarily many brackets. For example, no need to write f (g (x)) or (f x) + (g y), since f (g x) and f x + g y suffice.
- Further brackets can sometimes be saved by using the \$ operator, for example writing f \$ g x \$ h y instead of f (g x (h y)).
- The tool hlint gives warnings about redundant brackets, as well as about overuse of \$.

- Haskell has various number types: Int, Integer, Float, Double, Rational, ...
- Number literals can have a different concrete type depending on context, e.g., 3 :: Int, 3 :: Float, 3.5 :: Float, 3.5 :: Double
- For general expressions there are overloaded conversion functions, for example fromIntegral with, among others, any of the types Int -> Integer, Integer -> Int, Int -> Rational, ..., and truncate, round, ceiling, floor, each with any of the types Float -> Int, Double -> Integer, ...

... and arithmetic operators

 Operators are also overloaded, and often no conversion is necessary, for example in 3 + 4.5 or also in:

> f x = 2 * x + 3.5g y = f 4 / y

 In other cases, conversion <u>is</u> necessary, for example in this:

f :: Int -> Float
 f x = 2 * fromIntegral x + 3.5
or:
 f x = 2 * x + 3.5
 g y = f (fromIntegral (length "abcd")) / y

- Some operators are available only at certain types, e.g., no division symbol "/" on integer types.
- Instead, the function div :: Int -> Int -> Int (also on Integer).
- Binary functions (not just arithmetic ones) can be <u>used</u> like operators, for example writing 17 `div` 3 instead of div 17 3.
- Useful mathematical constants and functions exist, e.g., pi, sin, sqrt, min, max, ...

Other pre-existing types:

- Type Bool, with values True and False and operators &&, ||, and not.
- Type Char, with values 'a', 'b', ..., '\n' etc., and functions succ, pred, as well as comparison operators.
- List types: [Int], [Bool], [[Int]], ..., with various pre-defined functions and operators.
- Character sequences: type String = [Char], with special notation "abc" instead of ['a', 'b', 'c'].
- Tuple types: (Int, Int), (Int, String, Bool), ((Int, Int), Bool, [Int]), also [(Bool, Int)] etc.

- You should really not be "afraid" to use if-then-else
- as subexpressions (e.g., as arguments to functions).
- There is no reason to write something like
 if b == True then ... else ...
 since
 if b then ... else ...
 means the same thing.
- Also, this:

check x y = if x < y then True else False
is a rather complicated way of just saying this:
 check x y = x < y</pre>

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 It is always a good idea to write down type signatures for top-level functions. Among other benefits, it saves you from having to deal with (errors involving) types like: fun :: (Floating a, Ord a) => a -> a

 In case of doubt concerning number conversions, it usually does not hurt to add some fromIntegralcalls, which in the worst case will be no-ops (since, among others, fromIntegral :: Int -> Int).

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If you have repeated occurrences of a common subexpression, share them! For example, instead of this:

```
scene t =
    if 8 * sin t > 0
    then translate (8 * \cos t) (8 * \sin t) \dots
    else ...
rather write this:
 scene t =
    let x = 8 * \cos t
        y = 8 * sin t
    in if y > 0 then translate x y ... else ...
```

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If the hlint tool mentions "eta reduction", here is was it means:

Instead of something like:

ball :: Double -> Picture
ball t = solidCircle t

one might just as well write:

ball :: Double -> Picture

ball = solidCircle

• Also consider:

opening :: Double -> Picture
opening = rectangle 10

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Programming by case distinction

Expressing conditional behaviour

- We have already discussed if-then-else repeatedly, both in lecture and exercises.
- Other ways you may have seen or already used are list comprehensions without generators:
 - pictures [moon | hour > 22 | hour < 5]
 - \equiv if hour > 22 || hour < 5

```
then moon
else blank
```

• ... and indirect conditionality via mathematical functions:

```
rotated (min t pi) ...
```

```
≡ if t < pi
```

```
then rotated t ...
```

```
else rotated pi ...
```

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• ... and function definition using guards:

scene t
 t <= pi = ...
 pi < t && t <= 2 * pi = ...
 2 * pi < t = ...</pre>

• This is again similar to mathematical notation:

$$f(x) = \begin{cases} 0, & \text{if } x \le 0 \\ x, & \text{if } 0 < x \le 1 \\ 1, & \text{if } x > 1 \end{cases}$$

• Let us discuss some details based on this example:

- First of all, what about the order of clauses?
- Well, in this example, the following variant is equivalent:

Function definition using guards

- What if the guard conditions overlap?
- Then this is okay:

but this is problematic:

• Always the first matching clause is used!

• Even with the "correct" order:

we can have problems with some inputs.

• If no clause matches, we get a runtime error!

- In fact, if called with appropriate settings, the compiler warns us of this possible runtime error ahead of time.
- We can avoid both the warning and the actual nonexhaustiveness error at runtime by having a "catch-all" clause:

Function definition using guards

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• In this specific case, negative inputs would still be a problem.

• Which we could remedy as follows:

• Some lessons: order matters (and can be exploited), exhaustiveness matters. Also, some further aspects...

Function definition using guards

- The compiler's checks ahead of time are nice, but necessarily not perfect.
- For example, it cannot in general detect infinite recursion ahead of time. (The Halting Problem!)
- Even the "simpler" static exhaustiveness checks are not as powerful as one might sometimes hope.
- For example, one might hope that something like this:

is statically determined safe. But no (and for good reason). So it is usually better to use an explicit otherwise clause.

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• Also, the more desirable "fix" to the issue of possible negative inputs for

(instead of switching to n <= 0 in the first clause) would be to statically prevent negative inputs from occurring at all, via the type system.

• But that is a topic for a later lecture.

Function definition using guards

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• For now, let us apply our insights to this situation considered earlier:

• Here is how this should probably look instead:

Some further syntactic variations:

```
factorial :: Integer -> Integer
factorial n | n == 0 = 1
factorial n | otherwise = n * factorial (n - 1)
factorial :: Integer -> Integer
factorial n | n == 0 = 1
factorial n = n * factorial (n - 1)
factorial :: Integer -> Integer
factorial 0 = 1
factorial n = n * factorial (n - 1)
```

Another example:

ackermann :: Integer -> Integer -> Integer ackermann 0 n | n >= 0 = n + 1 ackermann m 0 | m > 0 = ackermann (m - 1) 1 ackermann m n | m > 0 && n > 0 = ackermann (m - 1) (ackermann m (n - 1))

This one gives some interesting non-exhaustiveness warnings.

General rules for function definitions:

- One or more equations, with or without guards.
- One or more arguments; so far, only variable names (can be anonymous) or constants.
- Uniqueness of variable names within one equation.
- Never expressions, in argument position at definition sites, that would require computation or "solving".

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A few more examples:

```
not :: Bool -> Bool
not True = False
not _ = True
(\&\&) :: Bool -> Bool -> Bool
True && True = True
     && _ = False
(\&\&) :: Bool -> Bool -> Bool
b \& True = b
_ && _ = False
```

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Working with lists

- We will consider a lot of examples in the lecture and exercises that deal with lists.
- But that is mostly for didactical reasons. In the "real world", there are often more appropriate data structures (and we will eventually see how to define them ourselves).
- In part due to historical precedent (Lisp), Haskell has a very rich library of list processing functions.
- It also has specific syntactical support for lists (e.g., list comprehensions).
- As already mentioned, Haskell lists are homogeneous.

Examples of existing (first-order) functions on lists

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take 3 [110]	==	[1,2,3]
drop 3 [110]	==	[4,5,6,7,8,9,10]
null []	==	True
null "abcde"	==	False
length "abcde"	==	5
head "abcde"	==	'a'
last "abcde"	==	'e'
tail "abcde"	==	"bcde"
init "abcde"	==	"abcd"
splitAt 3 <mark>"abcde"</mark>	==	("abc","de")
"abcde" !! 3	==	'd'
reverse "abcde"	==	"edcba"
"abc" ++ "def"	==	"abcdef"
zip "abc" "def"	==	[('a','d'),('b','e'),('c','f')]
concat [[1,2],[],[3]]	==	[1,2,3]

Essentially Quicksort:

```
sort :: [Integer] -> [Integer]
sort [] = []
sort list =
  let
  pivot = head list
  smaller = [ x | x <- tail list, x < pivot ]
  greater = [ x | x <- tail list, x >= pivot ]
  in sort smaller ++ [ pivot ] ++ sort greater
```

• In Haskell there are even expressions and values for infinite lists, for example:

[1,3..] = [1,3,5,7,9,...][n^2 | n <- [1..]] = [1,4,9,16,...]

• And while we of course cannot print complete such lists, we can still work normally with them, as long as the ultimate output is finite:

But there is no mathematical magic at work, so for example this:

 $[m | m < - [n^2 | n < - [1..]], m < 100]$

will "hang" after producing a finite prefix.

Why is that, actually?

Discussion: referential transparency!

• "Functional languages excel at wholemeal programming, a term coined by Geraint Jones. Wholemeal programming means to think big: work with an entire list, rather than a sequence of elements; ..." Ralf Hinze

 "Wholemeal programming is good for you: it helps to prevent a disease called indexitis, and encourages lawful program construction."

Richard Bird

- An example: Let us assume we want to multiply each element of an array or list by its position in that data structure, and sum up over all the resulting values.
- It seems fair to say that this is a typical solution in C:

```
int array[n];
int result = 0;
for (int i = 0; i < n; i++)
result = result + i * array[i];
```

• And that is about okay, but it does suffer from indexitis.

• The same example, in a wholemeal fashion, in Haskell:

sum [i * v | (i, v) <- zip [0..] list]</pre>

- Nice, short, declarative.
- Of course, one could consider this cheating, because it is using a conveniently predefined function sum.
- But actually, that is beside the point. Even without that convenience function, it would not have taken more than a dozen keystrokes to express the summation.
- And using a convenient array sum function would not exactly have made the C version any nicer than it is.

- So let us discuss the actual issues, expressivity and susceptibility to change and refactoring.
- Say, what if we decided that the counting of positions should start at 1 instead of 0?
- In the C version, that could mean we would switch from this:

```
for (int i = 0; i < n; i++)
result = result + i * array[i];</pre>
```

to:

```
for (int i = 1; i <= n; i++)
  result = result + i * array[i-1];</pre>
```

• Indexitis!

• In the Haskell version, we simply switch from:

sum [i * v | (i, v) <- zip [0..] list]</pre>

to:

sum [i * v | (i, v) <- zip [1..] list]</pre>

• To be fair again, in C we could have made a different edit:

for (int i = 0; i < n; i++)

result = result + (i+1) * array[i];

• But actually, that is just indexitis in a different form.

- The fundamental issue in the C version is a lack of conceptual separation of values to enumerate/process on the one hand, and loop control on the other hand.
- Whereas the Haskell version has that separation in the zip [k..] ... expression.
- Basically, the Haskell version needs no explicit loop control, it does not access data structure elements by index (remember what I said about avoiding use of the !! operator whenever possible), and it does not need to increment a loop counter or talk about the "loop end" condition (because: infinite lists).

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- Okay, but are we fooling ourselves, efficiency-wise?
- Certainly, code like

for (int i = 0; i < n; i++)
result = result + i * array[i];</pre>

is more efficient than

sum [i * v | (i, v) <- zip [0..] list]</pre>

because it does not need to use extra memory, and does not need several data structure traversals?

- Well, no. Actually, a compiler can translate the declarative code into a tight C-like loop, not using an intermediate data structure, just fine.
- A compiler can even spot parallelization opportunities, thanks to the "independent values" aspect we already discussed when comparing list comprehensions against for-loops in an earlier lecture.
- That all has to do also with the "lawful program construction" aspect from the Richard Bird quote.
- We could also talk more about refactoring...
- But is what we saw for the somewhat artificial example now representative of real situations? Claim: Yes!

- Let us do a live exercise in wholemeal programming. (Warning: not a "real situation" either, just as most exercises in this course.)
- Say we want to write a function that takes a list and removes adjacent duplicates:

compress [1,3,3,3,2,4,4,2] == [1,3,2,4,2]

- And we want to do this without accessing list elements by index, without cutting the list into pieces and working on parts, etc. (no "piecemeal programming").
- Also, we want to be good software engineers, so ...

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Polymorphic types

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• Remember that each Haskell list is homogeneous, i.e., cannot contain elements of different types.

"abc"	::	[Char]
[1,2,3]	::	[Integer]
['a',2]		ill-typed

 At the same time, functions and operators on lists can be used quite flexibly:

reverse "abc"	== "cba"
reverse [1,2,3]	== [3,2,1]
"abc" ++ "def"	== "abcdef"
[1,2] ++ [3,4]	== [1,2,3,4]

• We have already depended on this flexibility a lot!

- So there should be a way to reconcile the rigidity of types with flexible use of functions.
- We want to be able to write

"abc" ++ "def" and [1,2] ++ [3,4], as well as

elem 2 [1,2] and elem 'c' "ab",

but at the same time prevent calls like

"ab" ++ [3,4] and elem 'a' [1,2,3].

- So what are the types of functions like those seen?
- We do not have, and clearly do not want, different functions like reverseChar :: [Char] -> [Char] and reverseInteger :: [Integer] -> [Integer].
- Instead, we use type variables, as in:

reverse :: [a] -> [a]

That is not, at all, like being untyped. For example, the type (++) :: [a] -> [a] -> [a] does not mean that "anything goes".
(Still not possible to write this: "ab" ++ [3,4].)

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• We have already seen a lot of functions that fit this pattern:

head	::	[a] -> a
tail	::	[a] -> [a]
last	::	[a] -> a
init	::	[a] -> [a]
length	::	[a] -> Int
null	::	[a] -> Bool
concat	::	[[a]] -> [a]

 In concrete applications, the type variable gets instantiated appropriately: head "abc" :: Char.

Polymorphic functions on lists

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- Of course, a polymorphic function does not need to be polymorphic in <u>all</u> its arguments.
- For example:

(!!) :: [a] -> Int -> a
take :: Int -> [a] -> [a]
drop :: Int -> [a] -> [a]
splitAt :: Int -> [a] -> [a]

• And what about zip?

- The function zip also takes homogeneous lists as arguments.
- But unlike the case of (++), where we want to allow "ab" ++ "cd" and [1,2] ++ [3,4], but to disallow "ab" ++ [3,4], for zip we want to allow all of the following:

zip "ab" "cd" zip [1,2] [3,4] zip "ab" [3,4]

So the type cannot be like that for (++):

 [a] -> [a] -> ...

• Instead:

- Different type variables can be, but do not have to be, instantiated by different types.
- Hence, all of these make sense:

zip "ab" "cd"	$a = Char$, $b = Char$
zip [1,2] [3,4]	a = Int, b = Int
zip "ab" [3,4]	a = Char, b = Int

Whereas a mixed call for (++) does not:
 "ab" ++ [3,4] -- a = Char or Int?

Polymorphic functions in other languages

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- Have you seen something like those types in another language before?
- Example in Java with Generics:

<T> List<T> reverse(List<T> list)
{ ... }

```
corresponding to:
```

```
reverse :: [a] -> [a]
reverse list = ...
```

Inference of polymorphic types

- One aspect (among several) that distinguishes polymorphism in Haskell and its FP predecessors from those other languages is type inference.
- We need not declare polymorphism, since the compiler will always infer the most general type automatically.
- For example, for f (x,y) = x the compiler infers
 f :: (a,b) -> a.

Consequences of polymorphic types

- Polymorphism has really interesting semantic consequences.
- For example, in an earlier lecture, I mentioned that always:

reverse [f x | x <- xs] \equiv [f x | x <- reverse xs]

- What if I told you that this holds, for arbitrary f and xs, not only for reverse, but for any function with type
 [a] -> [a], no matter how it is defined?
- Can you give some such functions (and check the above claim)?



• Recall that in the earlier lecture the reverse-claim occurred in the context of comparing, in the imperative world, this:

vs. this:

• Not only are these two loops not necessarily equivalent, but even when imposing conditions under which they are, we do not get an as general and readily applicable law as just seen in the declarative world.

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Higher-order functions

- So far, we have mainly dealt with first-order functions, that is, functions that take "normal data" as input arguments and ultimately return some value.
- But we have also already seen functions to which we passed other functions as arguments. For example, quickCheck and animationOf.
- Indeed, let us take a look at the type of the latter: animationOf :: (Double -> Picture) -> IO ()

• Note: Every function is a (mathematical) value, but not every value is a function.

• The type

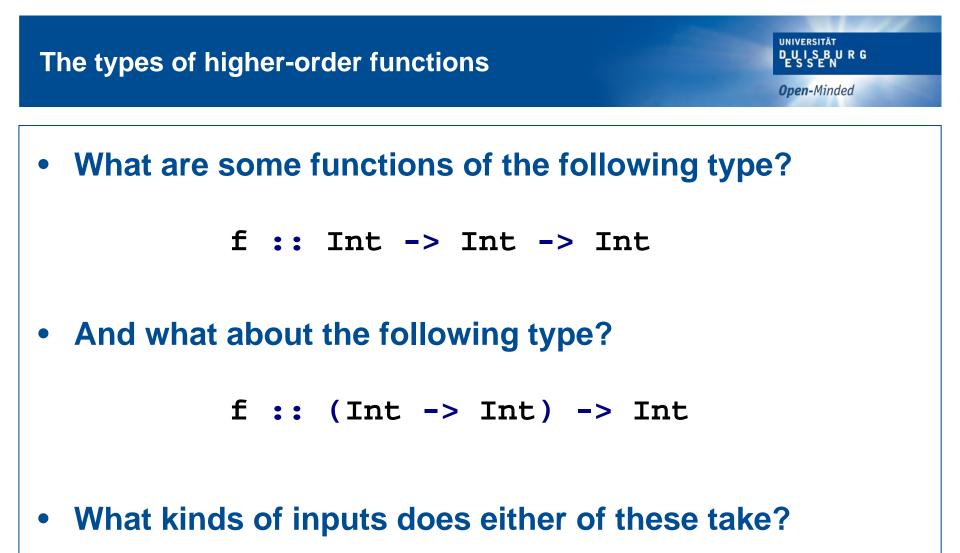
animationOf :: (Double -> Picture) -> IO ()

means something completely different than the type

animationOf :: Double -> Picture -> IO ()

• Indeed, parentheses in such places are very significant.

• Let us discuss this based on a simpler example type.



• And what can they do with their inputs?

- Where do we get functions from that we can pass as arguments to higher-order functions?
- Well, in Haskell functions are almost everywhere, right? So we should not have any shortage of supply.
- Of course, there are many predefined functions already.
- We could also use functions we have explicitly defined on the top level of our program (such as passing your own scene function to animationOf).
- Or partial applications of any of those. For example,
 (+) :: Int -> Int -> Int, and as a consequence,
 (+) 5 :: Int -> Int.

- Indeed, the type Int -> Int -> Int could be read as Int -> (Int -> Int).
- But those parentheses can be omitted.
- Two viewpoints here: a function that takes two Int values and returns one Int value, or a function that takes one Int value and returns a function that takes one Int value and returns one Int value.
- Both viewpoints are valid! No difference in usage (thanks to Haskell's function application syntax).
- Another syntactic specialty: so-called "sections". For example, "(+) 5" can be written as "(5 +)".

- We can also syntactically create new functions "on the fly", instead of predefined or own, explicitly defined and named, functions already in the program.
- Such anonymous functions use the so-called lambdaabstraction syntax (which we have already seen in the context of QuickCheck tests): \x -> x + x

So, some options of functions we could pass to a function f :: (Int -> Int) -> Int are:
 id, succ, gregorianMonthLength 2018, (- 5),
 \x -> x + x, \n -> length [1..n]

- The lambda-abstraction syntax also allows us to get a clearer view on Haskell's function definition syntax (and its choice to be different from standard mathematical function definition syntax).
- Namely, the following four definitions are equivalent (each of type add :: Int -> Int -> Int):

add x y = x + y add x = $y \rightarrow x + y$ add = $x \rightarrow y \rightarrow x + y$ add = $x \rightarrow y \rightarrow x + y$

 With standard mathematical notation, add(x,y) = , such variations would not have been so fluent. • If we do want, on some occasion, to work with tupled argument functions, we can "convert" back and forth in a very general way:

curry :: $((a,b) \rightarrow c) \rightarrow (a \rightarrow b \rightarrow c)$ curry f = $x y \rightarrow f(x,y)$

uncurry :: $(a \to b \to c) \to ((a,b) \to c)$ uncurry f = $(x,y) \to f x y$

• A typical use would be if we want to pass some function to a higher-order function, but it currently is of the "wrong form" (tupled vs. untupled).

- But is any of that really useful to us?
- The examples so far look somewhat esoteric and artificial, except maybe for the animationOf and quickCheck "drivers", which we do not know how to write ourselves yet though, anyway (due in part to the involvement of IO).

• Well, there are many immediately useful higher-order functions on lists as well...

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Higher-order functions on lists

• For example, the function

foldl1 :: (a -> a -> a) -> [a] -> a

puts a (left-associative) function/operator between all elements of a non-empty list.

• So to compute the sum of such a list:

foldl1 (+) [1,2,3,4]

which will expand to:

1 + 2 + 3 + 4

• Another useful function:

map :: (a -> b) -> [a] -> [b]

which applies a function to all elements of a list.

• For example:

map even [1..10]

map (dilated 5) [pic1, pic2, pic3]

• And another one:

filter :: (a -> Bool) -> [a] -> [a]

which selects list elements that satisfy a certain predicate.

• For example,

filter isPalindrome completeDictionary

filter (> 0.5) bonusPercentageList



• While the following are not the actual definitions of map and filter, we can think of them as such:

map :: (a -> b) -> [a] -> [b]
map f list = [f a | a <- list]</pre>

filter :: (a -> Bool) -> [a] -> [a] filter p list = [a | a <- list, p a]

 Conversely, <u>every</u> list comprehension expression, no matter how complicated with several generators, guards, etc., can be implemented via map, filter, and concat.

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- Is programming with map and filter (and fold11 and the like) still "wholemeal programming", which is what we have mostly used list comprehensions for so far?
- Yes, absolutely. In a sense even more so, since higherorder functions provide a further step in the direction of more abstraction.

• For example, if we want to square some numbers from a given list, subject to the condition that we are specifically interested in numbers divisibly by four, but still have to work out whether we want to check this divisibility before or after squaring, then ...



... with list comprehensions we would consider, and maybe experiment with,

While with map and filter we would simply decide between

• Also, a law like (mentioned earlier):

reverse [f x | x <- xs] \equiv [f x | x <- reverse xs]

can nicely be expressed as:

reverse . map f \equiv map f . reverse

• Then we can also ask under which conditions this holds:

filter p . map $f \equiv map f$. filter q

• Generally, higher-order functions are a boon for "lawful program construction" (see the Richard Bird quote).

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Algebraic data types

- We have so far seen various types on which functions can operate, such as number types (Int, Float, ...), other base types like Bool and Char, as well as list and tuple constructions to make compound types, arbitrarily nested ([...], (...,..)).
- We have also seen that libraries can apparently define their own, domain specific types, such as Picture.
- To do the same ourselves: algebraic data types.
- These are a more general and more stringent version of what is usually know as enumeration or union types. They are also the inspiration for features like Swift's (recursive) enum types.

- Let us start simple. Assume we want to be able to talk about days of the week, and compute things like "this is a workday, yes/no".
- We could fix some encoding of Monday, Tuesday etc. as numbers (e.g., Monday = 1, Tuesday = 2, ...) and define functions like:

workday :: Integer -> Bool workday d = d < 6

• In a sense, we were lucky here that the intended property corresponds to number ranges 1–5 and 6–7.

Simple enumeration types

- So let us try to instead express on which days of the week there is some activity (lecture or exercise session) in the ProPa course.
- The answer this time is not a simple arithmetic comparison like d < 6, but we can for example implement:

```
propaDay :: Integer -> Bool
propaDay 4 = False
propaDay 6 = False
propaDay 7 = False
propaDay _ = True
```

 In either case, what if we call workday or propaDay with an input like 12?



```
data Day
= Monday | Tuesday | Wednesday | Thursday
| Friday | Saturday | Sunday
```

• Now:

propaDay :: Day -> Bool
propaDay Thursday = False
propaDay Saturday = False
propaDay Sunday = False
propaDay _ = True

... and it is impossible to pass illegal inputs (like 12th day).

• Terminology: type constructors and data constructors.

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Simple enumeration types

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- In addition to excluding absurd inputs, we get more useful exhaustiveness (and also redundancy) checking.
- For example, remember the game level example:

```
level :: (Integer, Integer) -> Integer
aTile :: Integer -> Picture
aTile 1 = block
aTile 2 = pearl
aTile 3 = water
aTile 4 = air
aTile = blank
```

• Imagine that we introduce a new kind of tile, produce its new "number code" inside the level-function, but forget to also handle it in the aTile-function. No compiler warning!

If we had instead introduced a new type:
<mark>data</mark> Tile = Blank Block Pearl Water Air
and used level :: (Integer, Integer) -> Tile
and: aTile :: Tile -> Picture
aTile Blank = blank
aTile Block = block
aTile Pearl = pearl
aTile Water = water
aTile Air = air

then adding another value to data Tile could not go unnoticed in aTile.

The compiler would actually warn us if we forgot to handle the new value there!

- Going beyond simple enumeration types, algebraic data types can encapsulate additional values in the alternatives.
- That is, the data constructors can take arguments.
- For example:

• A possible value of type Connection:

Train (Date 20 04 2011) (Hour 11) (Hour 14)

• Computation on such types is via <u>pattern-matching</u>:

• At the same time, the data constructors are also normal functions, for example:

Date :: Int -> Int -> Int -> Date

Train :: Date -> Time -> Time -> Connection



• Algebraic data types can be recursive. For example:

data Nat = Zero | Succ Nat

• Values of this type:

Zero, Succ Zero, Succ (Succ Zero), ...

Computation by recursive function definitions:

```
add :: Nat -> Nat -> Nat
add Zero m = m
add (Succ n) m = Succ (add n m)
```

• With several recursive occurrences, tree structures:

data Tree = Leaf | Node Tree Int Tree

• Values: Leaf, Node Leaf 2 Leaf, ...

• Computation:

```
height :: Tree -> Integer
height Leaf
= 0
height (Node left _ right)
= 1 + max (height left) (height right)
```



Just like functions, algebraic data types can be polymorphic:

• Another example, from the standard library:

```
data Maybe a = Nothing | Just a
```

- Popular for functions that would otherwise be partial.
- Such as also in a re-design of the game level example:

```
data Tile = Block | Pearl | Water | Air
level :: (Integer, Integer) -> Maybe Tile
aTile :: Tile -> Picture
aTile Block = block
aTile Pearl = pearl
aTile Water = water
aTile Air = air
```

- Note that, just as any other data in Haskell, values of algebraic data types are immutable.
- For example, we do not <u>change</u> any tree in a function like this:

• Discuss what this means ...

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Lists as algebraic data type

Another example data structure	UNIVERSITÄT DUISBURG ESSEN
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 If Haskell did not yet have a list type, we could implement one ourselves: 	
data List a = Nil Cons a (List	ca)
• Example value: Cons 1 (Cons 2 Nil) :	List Int
Computation:	

length :: List a -> Int
length Nil = 0
length (Cons _ rest) = 1 + length rest



• In fact, modulo special syntax, that is exactly what Haskell lists are:

data [a] = [] (:) a [a]

 So, for example, [1,2] is simply 1: (2:[]), which thanks to right-associativity of ":" can also be written as 1:2:[].

 Functions on lists can then, of course, also be defined using pattern-matching.

Some example functions:

```
length :: [a] -> Int
length [] = 0
length (_:rest) = 1 + length rest
append :: [a] -> [a] -> [a]
append [] ys = ys
append (x:xs) ys = x : append xs ys
head :: [a] -> a
head (x:_) = x
zip :: [a] -> [b] -> [(a,b)]
zip(x:xs)(y:ys) = (x,y) : zip xs ys
zip _
                 = []
```

- Note how clever arrangement of cases/equations can make function definitions more succinct.
- For example, we might on first attempt have defined zip as follows:

zip :: [a] -> [b] -> [(a,b)]
zip [] _ = []
zip (x:xs) [] = []
zip (x:xs) (y:ys) = (x,y) : zip xs ys

- But the version from the previous slide is equivalent.
- Both versions also work with infinite lists, btw.

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Also, as another example of a function we have used:

```
map :: (a -> b) -> [a] -> [b]
map f [] = []
map f (x:xs) = f x : map f xs
```

And indeed related:

```
treeMap :: (a -> b) -> Tree a -> Tree b
treeMap f Leaf = Leaf
treeMap f (Node left x right)
   = Node (treeMap f left)
        (f x)
        (f x)
        (treeMap f right)
```

• Also remember the function

foldl1 :: (a -> a -> a) -> [a] -> a

which puts a (left-associative) function/operator between all elements of a non-empty list.

• It is a member of a whole family of related functions, the most prominent of which is foldr, defined thus:

foldr :: (a -> b -> b) -> b -> [a] -> b
foldr _ c [] = c
foldr f c (x:xs) = f x (foldr f c xs)

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More on pattern-matching

Evaluation by pattern-matching

- Ultimately, pattern-matching is what drives (lazy) evaluation in Haskell.
- For example, let us consider how the expression

head (tail (f [3, 3 + 1]))

is evaluated, given the following function definitions (and the known head and tail functions):

Explicit case-expressions

- Pattern-matching is not restricted to the left-hand sides of function definitions, it can also occur in expressions, using the case-keyword.
- For example, instead of something like this:

if isNothing maybeValue
then ... something ...
else ... something else, using fromJust maybeValue ...

we can (and would usually prefer to) write this:

case maybeValue of Nothing -> ... something ... Just value -> ... something else, directly using value ...

- Pattern-matching always binds variable names that occur in patterns, possibly shadowing existing things of same name.
- That sometimes leads to confusion for beginners, such as why it does not work to write a function like the following one (given the existence of red :: Color etc., imported from CodeWorld):

primaryColor :: Color -> Bool
primaryColor red = True
primaryColor green = True
primaryColor blue = True
primaryColor _ = False

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Input / Output

"In short, Haskell is the world's finest imperative programming language."

Simon Peyton Jones

Input / Output in Haskell, general approach

- Even in declarative languages, there should be some (disciplined) way to embed "imperative" commands like "print something to the screen".
- In pure functions, no such interaction with the operating system / user / ... is possible.
- And clearly it should not be, since it would defy referential transparency.
- But there is a special do-notation in Haskell that enables interaction, and from which one can call "normal" functions.
- All the features and abstraction concepts (higher-order, polymorphism, ...) of Haskell remain available even in and with do-code.

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• Getting two numbers from the user and then printing some value computed from them to the screen:

• Note the (apparent) type inference on n and m.

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- There is a predefined type constructor IO, such that for every type like Int, Tree Bool, [(Int,Bool)] etc., the type IO Int, IO (Tree Bool), ... can be built.
- The interpretation of a type IO a is that elements of that type are not themselves concrete values, but instead are (potentially arbitrarily complex) sequences of input and output operations, and computations depending on values read in, by which ultimately a value of type a is created.
- An (independently executable) Haskell program overall always has an "IO type", usually main :: IO ().

- To actually create "IO values", there are certain predefined primitives (and one can recognize their IO-related character based on their types).
- For example, there are getChar :: IO Char and putChar :: Char -> IO ().
- Also, for several characters, getLine :: IO String and putStr, putStrLn :: String -> IO ().
- More abstractly, for any type for which Haskell knows (or was instructed) how to convert from or to strings, readLn :: Read a => IO a for input as well as print :: Show a => a -> IO () for output.



To combine IO-computations (i.e., to build more complex action sequences based on the IO primitives), we can use the do-notation.

Its general form is: do cmd_1

$$x_{2} < - cmd_{2}$$

$$x_{3} < - cmd_{3}$$

$$cmd_{4}$$

$$x_{5} < - cmd_{5}$$

where each cmd_i has an IO type and to each x_i (if present) a value of the type encapsulated in the cmd_i will be bound (for use in the rest of the do-block), namely exactly the result of executing cmd_i .

- The do-block as a whole has the type of the last cmd_n .
- For that last command, generally no \mathbf{x}_n is present.
- Often also useful (for example, at the end of a doblock): a predefined function return :: a -> IO a that simply yields its argument, without any actual IO action.
- What is never ever, at all, possible or allowed is to directly extract (beyond the explicit sequentialisation and binding structure within do-blocks) the encapsulated value from an IO computation, i.e., to simply turn an IO a value into an a value.

User defined "control structures"

- As mentioned, also in the context of IO-computations, all abstraction concepts of Haskell are available, particularly polymorphism and definition of higher-order functions.
- This can be employed for defining things like:

• Which can then be used thus:

```
while (< 10)
    (\n -> do {print n; return (n+1)})
    0
```